

Let  $y = 4 \sin[2(x - \frac{\pi}{3})] - 3$ . Fill in the blanks. Simplify your answers.

Middle  $y$ -value =     -3    

Phase shift =      $x = \frac{\pi}{3}$           $2(x - \frac{\pi}{3}) = 0$

Amplitude =     4         |4| 

Period =      $\pi$           $\frac{2\pi}{2}$

Maximum  $y$ -value =     1          $-3+4$

Quarter-period =      $\frac{\pi}{4}$     

Minimum  $y$ -value =     -7          $-3-4$

Find the  $x$ - and  $y$ - coordinates for all points corresponding to the middle, top and bottom of the graph of the function for 2 complete cycles, starting at the phase shift. State clearly if the point corresponds to the top, middle or bottom of the graph.

Point 1:  $x = \frac{\pi}{3}$      PHASE SHIFT      $y = -3$  (MID)     TOP, MIDDLE or BOTTOM

Point 2:  $x = \frac{4\pi}{12} + \frac{3\pi}{12} = \frac{7\pi}{12}$      PREVIOUS  $x$ -VALUE     QUARTER-PERIOD      $y = 1$  (TOP)     TOP, MIDDLE or BOTTOM

Point 3:  $x = \frac{7\pi}{12} + \frac{3\pi}{12} = \frac{10\pi}{12}$      PREVIOUS  $x$ -VALUE     QUARTER-PERIOD      $y = -3$  (MID)     TOP, MIDDLE or BOTTOM

Point 4:  $x = \frac{10\pi}{12} + \frac{3\pi}{12} = \frac{13\pi}{12}$      PREVIOUS  $x$ -VALUE     QUARTER-PERIOD      $y = -7$  (BOT)     TOP, MIDDLE or BOTTOM

Point 5:  $x = \frac{13\pi}{12} + \frac{3\pi}{12} = \frac{16\pi}{12}$      PREVIOUS  $x$ -VALUE     QUARTER-PERIOD      $y = -3$  (MID)     TOP, MIDDLE or BOTTOM

Point 6:  $x = \frac{16\pi}{12} + \frac{3\pi}{12} = \frac{19\pi}{12}$      PREVIOUS  $x$ -VALUE     QUARTER-PERIOD      $y = 1$  (TOP)     TOP, MIDDLE or BOTTOM

Point 7:  $x = \frac{19\pi}{12} + \frac{3\pi}{12} = \frac{22\pi}{12}$      PREVIOUS  $x$ -VALUE     QUARTER-PERIOD      $y = -3$  (MID)     TOP, MIDDLE or BOTTOM

Point 8:  $x = \frac{22\pi}{12} + \frac{3\pi}{12} = \frac{25\pi}{12}$      PREVIOUS  $x$ -VALUE     QUARTER-PERIOD      $y = -7$  (BOT)     TOP, MIDDLE or BOTTOM

Point 9:  $x = \frac{25\pi}{12} + \frac{3\pi}{12} = \frac{28\pi}{12}$      PREVIOUS  $x$ -VALUE     QUARTER-PERIOD      $y = -3$  (MID)     TOP, MIDDLE or BOTTOM

Let  $y = -2 \cos\left(\frac{\pi x}{8} + \frac{5\pi}{4}\right) + 3$ . Fill in the blanks. Simplify your answers.

Middle  $y$ -value = 3

Phase shift =

$x = -10$   $\frac{7\pi}{8} + \frac{5\pi}{4} = 0$   
 $\frac{8\pi x}{8} = -\frac{5\pi}{4} \cdot \frac{8}{\pi}$

Amplitude = 2  $1-21$  

Period =

16  $\frac{2\pi}{\frac{\pi}{8}} = 2\pi \cdot \frac{8}{\pi}$

Maximum  $y$ -value = 5  $3+2$

Quarter-period =

4

Minimum  $y$ -value = 1  $3-2$

Find the  $x$ - and  $y$ - coordinates for all points corresponding to the middle, top and bottom of the graph of the function for 2 complete cycles, starting at the phase shift. State clearly if the point corresponds to the top, middle or bottom of the graph.

Point 1:  $x =$  -10  
 PHASE SHIFT

$y =$  1 (BOT)  
 TOP, MIDDLE or BOTTOM

Point 2:  $x =$  -10 + 4 = -6  
 PREVIOUS QUARTER-  
 $x$ -VALUE PERIOD

$y =$  3 (MID)  
 TOP, MIDDLE or BOTTOM

Point 3:  $x =$  -6 + 4 = -2  
 PREVIOUS QUARTER-  
 $x$ -VALUE PERIOD

$y =$  5 (TOP)  
 TOP, MIDDLE or BOTTOM

Point 4:  $x =$  -2 + 4 = 2  
 PREVIOUS QUARTER-  
 $x$ -VALUE PERIOD

$y =$  3 (MID)  
 TOP, MIDDLE or BOTTOM

Point 5:  $x =$  2 + 4 = 6  
 PREVIOUS QUARTER-  
 $x$ -VALUE PERIOD

$y =$  1 (BOT)  
 TOP, MIDDLE or BOTTOM

Point 6:  $x =$  6 + 4 = 10  
 PREVIOUS QUARTER-  
 $x$ -VALUE PERIOD

$y =$  3 (MID)  
 TOP, MIDDLE or BOTTOM

Point 7:  $x =$  10 + 4 = 14  
 PREVIOUS QUARTER-  
 $x$ -VALUE PERIOD

$y =$  5 (TOP)  
 TOP, MIDDLE or BOTTOM

Point 8:  $x =$  14 + 4 = 18  
 PREVIOUS QUARTER-  
 $x$ -VALUE PERIOD

$y =$  3 (MID)  
 TOP, MIDDLE or BOTTOM

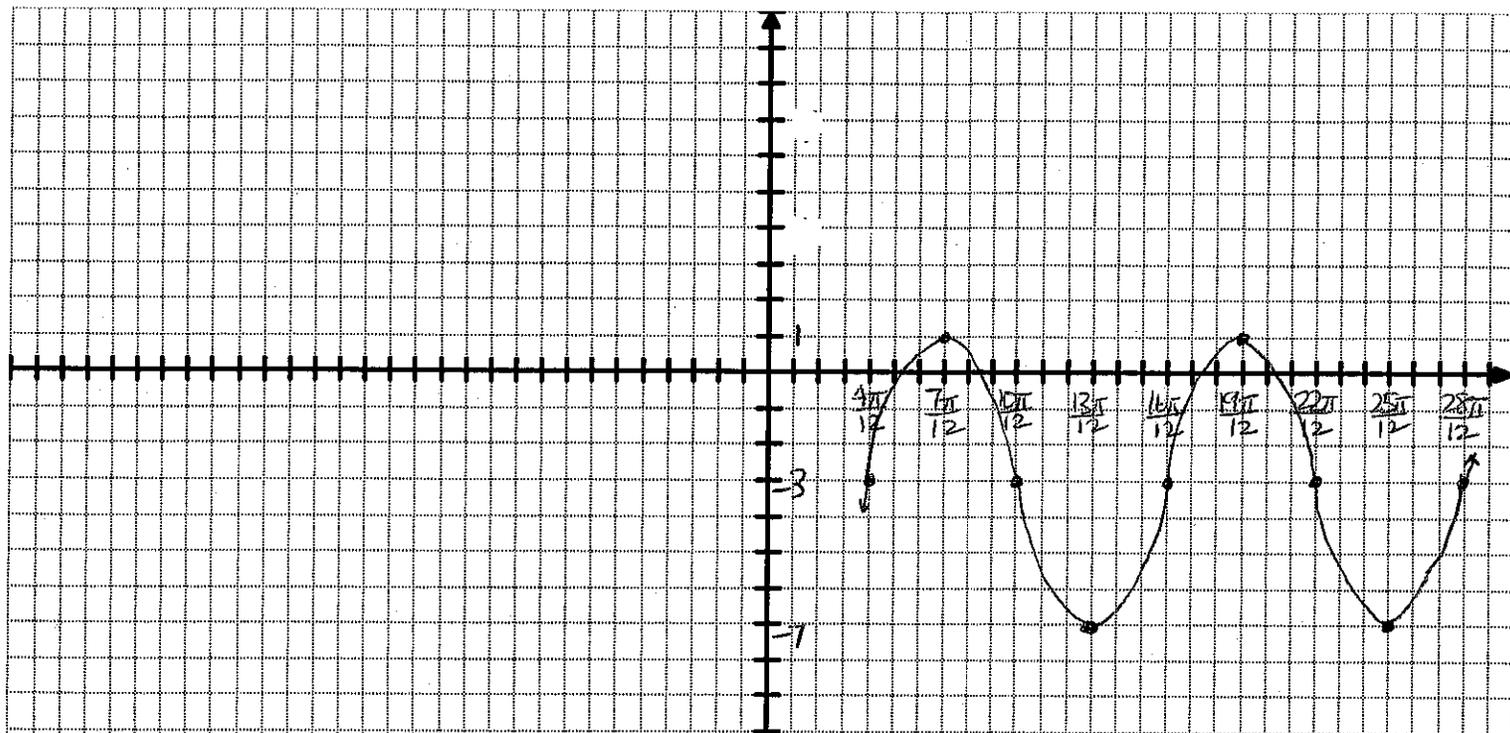
Point 9:  $x =$  18 + 4 = 22  
 PREVIOUS QUARTER-  
 $x$ -VALUE PERIOD

$y =$  1 (BOT)  
 TOP, MIDDLE or BOTTOM

Sketch a detailed graph of 2 complete cycles of  $y = 4 \sin[2(x - \frac{\pi}{3})] - 3$  using the information from Question 1 Part 1.

You must label all  $x$ - and  $y$ - values from Part 1 on the appropriate axes below, and you must use a consistent scale for each axis.

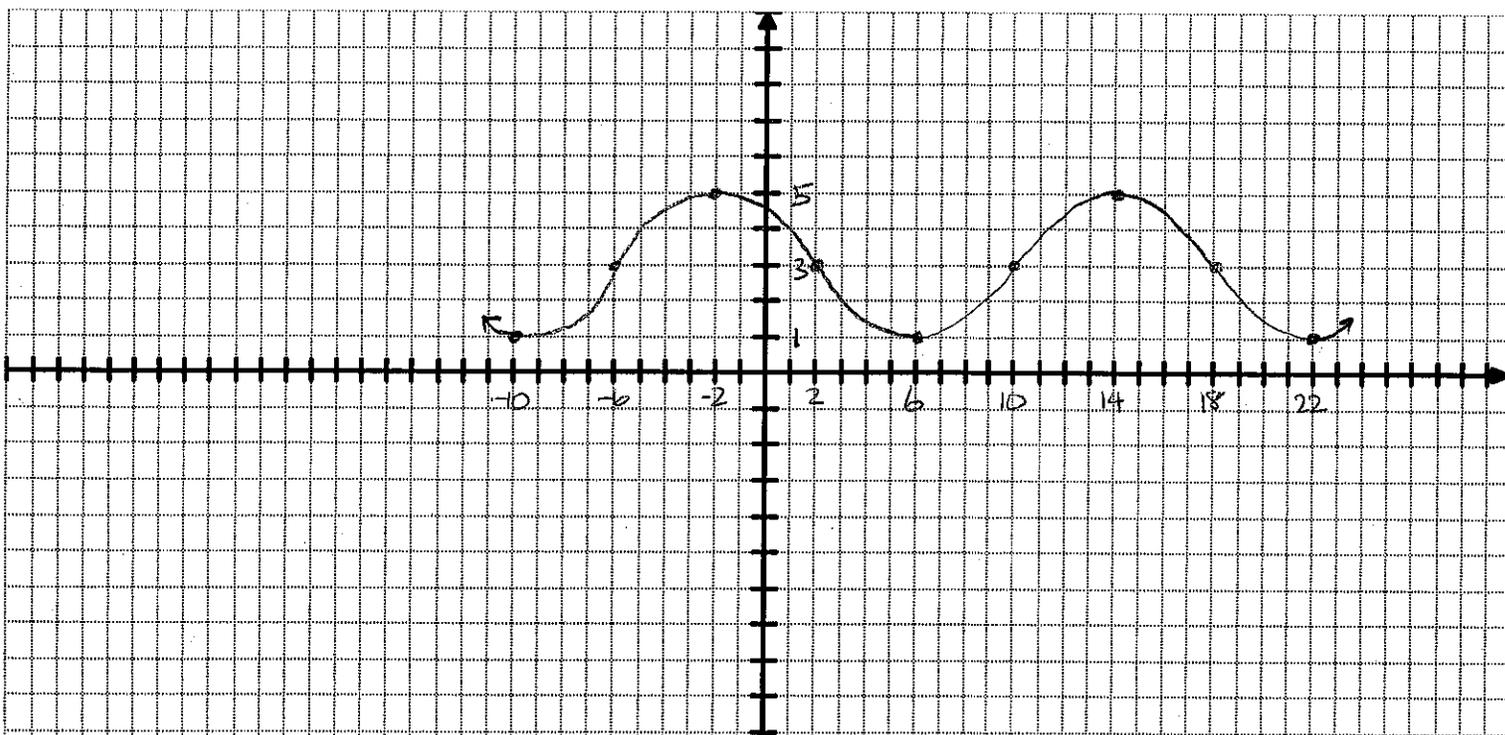
You do NOT need to label each tick mark on each axis, only the ones you found in Part 1.



Sketch a detailed graph of 2 complete cycles of  $y = -2 \cos(\frac{\pi x}{8} + \frac{5\pi}{4}) + 3$  using the information from Question 2 Part 1.

You must label all  $x$ - and  $y$ - values from Part 1 on the appropriate axes below, and you must use a consistent scale for each axis.

You do NOT need to label each tick mark on each axis, only the ones you found in Part 1.



Page 4: Question 3

Fill in the blanks regarding the graph on the right. Simplify your answers.

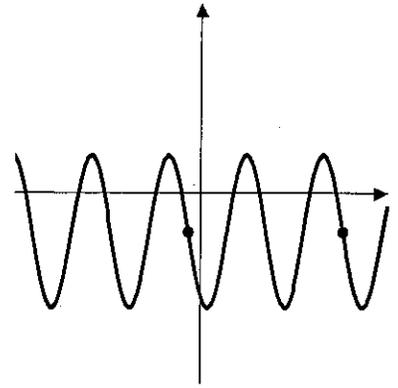
NOTE: The  $x$  - coordinates of the two points highlighted are  $-\frac{2\pi}{5}$  and  $2\pi$ , and correspond to points with the middle  $y$  - value.

The maximum and minimum  $y$  - values are 3 and  $-11$ .

Middle  $y$  - value = -4 = D  $\frac{3+(-11)}{2}$

Amplitude = 7 = |A|  $\frac{3-(-11)}{2}$

Phase shift =  $-\frac{2\pi}{5}$  = C  $-\frac{2\pi}{5}$



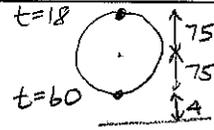
Period =  $2\pi - (-\frac{2\pi}{5}) = \frac{12\pi}{5}$   
 $\frac{6\pi}{5} = \frac{2\pi}{B} \Rightarrow B = \frac{5}{3}$   $B = \frac{2\pi \cdot 5}{6\pi \cdot 3}$

Given the points shown, the equation of the graph is easier to write using a NEGATIVE SIN function, POSITIVE or NEGATIVE SIN or COS

So,  $A =$  -7

The equation of the graph is  $y =$  -7 SIN  $\frac{5}{3}$   $(x -$   $-\frac{2\pi}{5}$  $) +$  -4 =  $-7 \sin \frac{5}{3}(x + \frac{2\pi}{5}) - 4$   
 A SIN or COS B C D

You are riding a ferris wheel with a radius of 75 feet, which is turning at a regular rate. You have a tremendous fear of heights, but you don't want to embarrass yourself in front of your date, so you try to distract yourself by finding an equation for your height ( $y$ ) as a function of time ( $t$ ).



At time  $t = 18$  seconds, you are at the top of the wheel. At time  $t = 60$  seconds, you are at the bottom of the wheel, which is 4 feet above the ground. (This is the first time you reach the bottom after time  $t = 18$  seconds.)

Fill in the blanks. Simplify your answers.

It may be helpful to draw a crude sketch of the height function and label the known  $t$  - and  $y$  - values on it.

Maximum  $y$  - value = 154

Phase shift = 18 = C

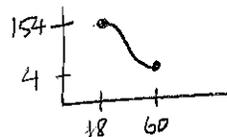
Minimum  $y$  - value = 4

Period =  $\frac{1}{2}P = 60 - 18 = 42$  84 =  $\frac{2\pi}{B}$

Middle  $y$  - value = 79 = D  $\frac{154+4}{2}$

$B = \frac{\pi}{42}$

Amplitude = 75 = |A|  $\frac{154-4}{2}$



Given the crude sketch of the height function, the equation is easier to write using a POSITIVE COS function, POSITIVE or NEGATIVE SIN or COS

So,  $A =$  75

The equation of the function is  $y =$  75 COS  $\frac{\pi}{42}$   $(t -$  18 $) +$  79.  
 A SIN or COS B C D